

Thoroughly Revised and Updated

Reasoning & Aptitude

for **GATE 2024**
and **ESE Pre 2024**

Comprehensive Theory *with* **Examples**
and **Solved Questions of**
GATE and ESE Prelims

Also useful for

UPSC (CSAT), MBA Entrance, Wipro, SSC, Bank (PO), TCS , Railways, Infosys,
various Public Sector Units and other Competitive Exams conducted by UPSC





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Reasoning & Aptitude for GATE 2024 & ESE Prelims 2024

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Director's Message

Engineering is one of the most chosen graduation fields, choosing to become an engineer after high school is usually a matter of interest but this eventually develops into “the purpose of being an engineer” and then a student thinks of cracking various competitive exams like ESE, GATE, PSUs exams, and other state engineering services exams. With the objective nature of these competitive exams and with increasing competition, it becomes necessary for the student to study and practice every topic and also get acclimatize with the style of questions asked in the exam.



Studying engineering in university is one aspect but studying to crack different prestigious competitive exams requires altogether different strategies, crystal clear concepts and rigorous practice of previous years' questions. Every student can achieve great results through proper guidance and exam-oriented study material, and hence we have come up with this book covering all the previous years' questions. This book will help aspirants to develop an understanding of important and frequently asked areas in the exam and will also help in strengthening concepts. MADE EASY Team has put sincere efforts in framing accurate and detailed explanations for all the previous years' questions. The explanation provided for each question is not only question specific but it will also give insight on the concept as a whole which will be beneficial for the student from the exam point of view to handle similar questions.

All the previous years' questions are segregated subject wise and further, they have been categorized topic-wise for easy learning and this certainly assists aspirants to solve all previous years' questions of a particular area in one place. I would like to acknowledge the efforts of the entire MADE EASY team who worked hard to solve previous years' questions with accuracy. I hope this book will stand up to the expectations of aspirants and my desire to serve the student community by providing the best study material will get accomplished.

B. Singh (Ex. IES)

CMD, MADE EASY Group

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A

Section

Arithmetic

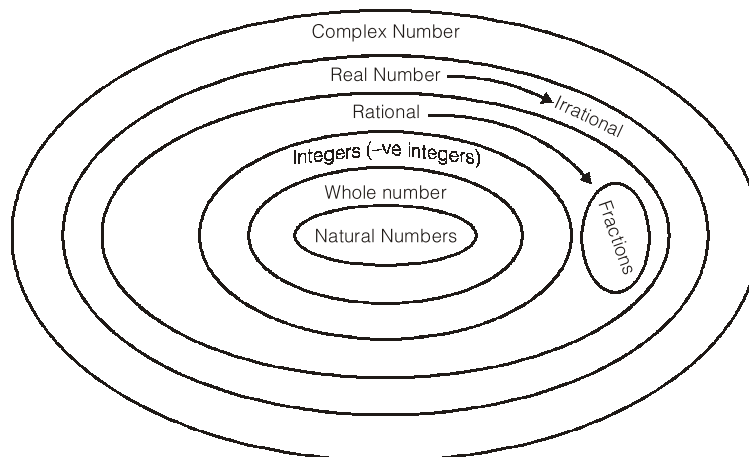
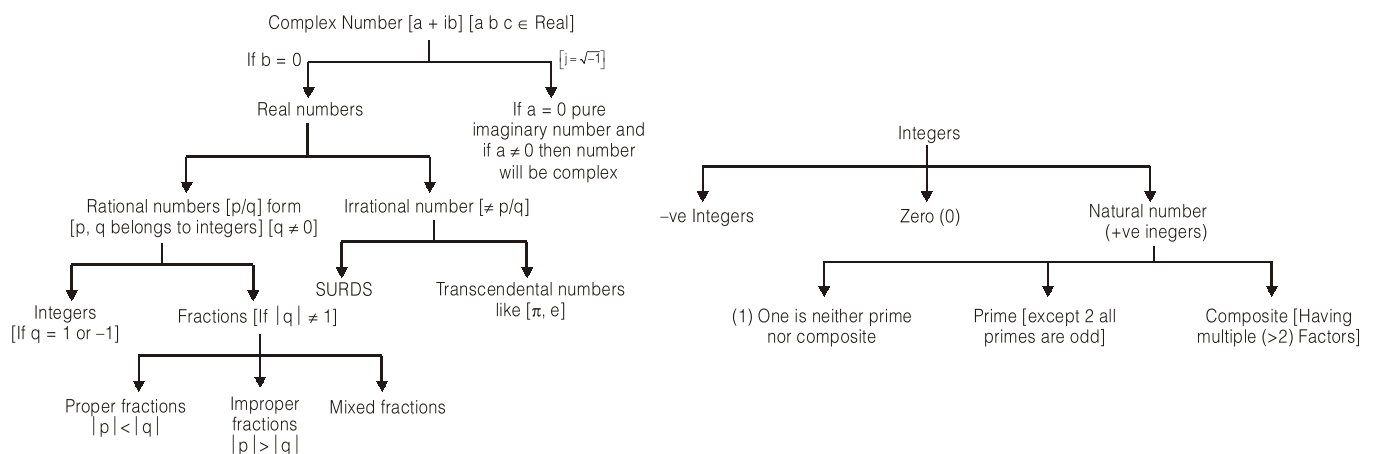
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CHAPTER

Number System

In Quantitative Aptitude (QA), Number System is one of the modules which is of critical importance. We can consider this module as the back bone as well as basic foundation and building block for QA as well as for reasoning. Applications of concepts of numbers can be easily found in puzzles, reasoning based questions, number series and many more reasoning areas. This is why it is our suggestion to students to understand the concepts discussed in the module thoroughly alongwith understanding of applications.

Classifications of Numbers



Our main focus in this module of numbers is on **real number system**. However in context of imaginary numbers only following property is important.

Imaginary Numbers

$$\begin{aligned}
 i &= \sqrt{-1} \Rightarrow i^{4K+1} \equiv \sqrt{-1} \equiv i \\
 i^2 &= -1 \Rightarrow i^{4K+2} \equiv -1 \equiv i^2 \\
 i^3 &= -i \Rightarrow i^{4K+3} \equiv -i \equiv i^3 \\
 i^4 &= 1 \Rightarrow i^{4K} \equiv 1 \equiv i^4
 \end{aligned}$$

Ex. 1

What is the value of expression

$$\frac{i^{12} + i^{13} + i^{14} + i^{15}}{i^{18} + i^{19} + i^{20} + i^{21}} ?$$

- (a) i^2 (b) -1
 (c) $1/i^2$ (d) None of these

Ans. (d)

$$\frac{i^{12}(1 + i + i^2 + i^3)}{i^{18}(1 + i + i^2 + i^3)}$$

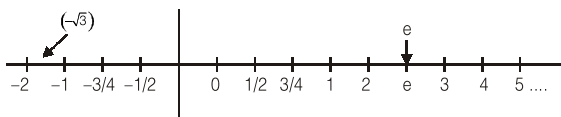
If we commit a mistake of cancelling out common terms in numerator and denominator options a, b, c all one correct hence my answer should be (d) but

$$\begin{aligned}
 \text{Expression } 1 + i + i^2 + i^3 \\
 = 1 + i + (-1) + (-i) = 0
 \end{aligned}$$

Hence expression in question leading to undetermined form $\left[\frac{0}{0}\right]$ hence correct answer is option (d).

Real Number System

Entire real numbers group of rational and irrational numbers combined forms the set of real number, which is represented by symbol $\rightarrow R$. All real numbers can be represented as points on a real number line.

**Rational Number**

All the numbers in p/q ($q \neq 0$) form are rational numbers [p, q are integers]. Set of rational number is represented by $\rightarrow Q$.

Rational Numbers have following forms of representations.

- (a) Terminating decimal forms

for example 0.125

$$\Rightarrow 0.125 = \frac{125}{1000} \Rightarrow \text{Rational}$$

- (b) Nonterminating but recurring decimal forms.

- (i) For example

$$Q = 0.37373737 \dots$$

$$100Q = 37.373737 \dots$$

$$99Q = 37 \Rightarrow Q = 37/99 \Rightarrow \text{rational}$$

- (ii) For example

$$Q = 0.37292929 \dots$$

$$100Q = 37.292929 \dots$$

$$10000Q = 3729.292929 \dots$$

$$9900Q = (3729 - 37)$$

$$Q = \left(\frac{3729 - 37}{9900} \right)$$

$$= \frac{p}{q} \text{ form} \Rightarrow \text{rational}$$

Fraction

All rational numbers in which $|q| \neq 1$ comprise the set of fractions.

Proper Fraction

$$\text{If } |p| < |q|$$

then fraction is proper fraction. Value of proper fraction is always in between $(-1 \text{ to } +1)$ i.e., $[-1 < p/q < 1]$

Improper Fraction

$$\text{If } |p| > |q|$$

then fraction is improper fraction. Value of improper fraction is < -1 or > 1 .

Mixed Fraction

Just a modified form of improper fraction.

$$\text{Eg. } \underbrace{\frac{13}{4}}_{\text{Improper fraction}} \Rightarrow \underbrace{3\frac{1}{4}}_{\text{equivalent mixed fraction}}$$

Integers

The set of all rational numbers in p/q form [$|q| = 1$] is called as integers. It is denoted by

$$I = \{ \dots, -3, -2, -1, 0, 1, 2, 3, \dots \}$$

It includes.

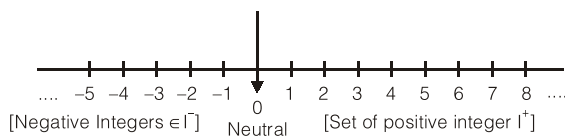
Negative Integers

$$I^- = \{ \dots, -7, -6, -5, -4, -3, -2, -1 \}$$

Positive Integers

$$I^+ = \{ 1, 2, 3, \dots \}$$

Note: Status of 0 (zero) is neutral neither positive nor negative.



Natural Numbers

All counting numbers or set of positive integers is considered as set of natural numbers. It denoted by set $[N \text{ or } I^+]$

$$N = \{1, 2, 3, 4, \dots\}$$

Whole Number

Set of all nonnegative integers are considered as whole number; it is denoted by set $W = \{0, 1, 2, 3, 4, \dots\}$

Note: If terms “numbers” is used without any qualifier than it means natural number henceforth.

Even Numbers & Odd Numbers

1. Even Numbers

All numbers divisible by 2 are considered as even numbers.

Note: Property evenness is applicable in entire integral number line. Hence $[-2, -4, -6, \dots]$ are even integers but they are not even numbers.

2. Odd Number

All numbers not divisible by 2 are odd.

$[1, 3, 5, 7, \dots]$ are odd numbers.

$[\dots, -5, -3, -1, \dots]$ are odd integers.

Properties of numbers based on even & odd

$$\text{Even} + \text{Even} = \text{Even}$$

$$\text{Odd} + \text{Odd} = \text{Even}$$

$$\text{Odd} + \text{Odd} + \text{Odd} = \text{Odd}$$

$$\text{Odd} \times \text{Odd} = \text{Odd}$$

$$\text{Odd} \times \text{Even} = \text{Even}$$

$$\text{Even} \times \text{Even} = \text{Even}$$

$$(\text{Even})^{\text{Odd}} \Rightarrow \text{Even}$$

$$(\text{Odd})^{\text{Even}} \Rightarrow \text{Odd}$$

$$(\text{Even})^{\text{Odd}} \Rightarrow \text{Even}$$

$$(\text{Odd})^{\text{Odd}} \Rightarrow \text{Odd}$$

These properties can be used extensively to find out alternative method to get answers quickly with the help of options. Here are few examples.

Ex. 1

There are two, 2-digit numbers ab and cd , ba is the another two digit number prepared by reversing the digits of ab , if $ab \times cd = 493$, $ba \times cd = 2059$, what is value ‘g’ sum of $(ab + cd) = ?$

- (a) 43 (b) 45
(c) 47 (d) 46

Ans: (d)

Value ‘g’ = $ab \times cd$ is odd.

It means ab and cd both are odd.

Hence there sum must be even, only one option is there which is even. Hence answer is option d.

Ex. 2

I have multiple gift vouchers of value, Rs. 101, 107, 111, 121, 131, 141, 151, 171. I have to pick exactly 10 vouchers to make payment of Rs. 1121. In how many ways I can do that?

- (a) one (b) two
(c) more than two (d) none of these

Ans. (d)

Reasoning is very simple, if I'll add 10 odd numbers their sum will be always even. Hence there is no way to accomplish this.

Prime Number & Composite Numbers

Prime Numbers

Number which are perfectly divisible either by 1 or by itself only are called prime numbers. 25 prime number are there which are less than 100. 2 is the only even prime number. All prime numbers greater than 5 can be expressed as $(6K \pm 1)$ ($K \in N$) form but all the numbers in form of $(6K \pm 1)$ form are not necessarily prime.

Composite Numbers

All the numbers which can be factorized into multiple prime numbers are called composite number.

Number (1) one is neither prime nor composite.

How to check whether given number is prime or not?

1. Take the square root of number
2. Consider the prime numbers, starting from 2 till the number. Take all prime numbers upto this square root value or nearest higher integer.

3. If number is divisible by any of these prime numbers, then number is composite.

Learn it by example:

Suppose we want to check, is 629 prime or not?
 Square root of 627 is just more than 25. Then prime no. till 25 are 2, 3, 5, 7, 11, 13, 17, 19, 23, 29.
 629 is not divisible by 2, 3, 5, 7, 11, 13 but is divisible by 17.
 Hence it is not prime number

One more example: 179

Square root of 179 is more than 13. Hence we need to check divisibility of 179 against 2, 3, 5, 7, 11, 13, 17
 179 is not divisible by either of these hence it is a prime number.

Test of Divisibility

1. Divisibility by 2

A number is divisible by 2 if the unit digit is zero or divisible by 2.
 Eg.: 22, 42, 84, 3872 etc.

2. Divisibility by 3

A number is divisible by 3 if the sum of digit in the number is divisible by 3.
 Eg.: 2553
 Here $2 + 5 + 5 + 3 = 15$, which is divisible by 3 hence 2553 is divisible by 3.

3. Divisibility by 4

A number is divisible by 4 if its last two digit are divisible by 4.
 Eg.: 2652, here 52 is divisible by 4 so 2652 is divisible by 4.
 Eg.: 3772, 584, 904 etc.

4. Divisibility by 5

A number is divisible by 5 if the units digit in number is 0 or 5.
 Eg.: 50, 505, 405 etc.

5. Divisibility by 6

A number is divisible by 6 if the number is even and sum of digits is divisible by 3.
 Eg.: 4536 is an even number also sum of digit $4 + 5 + 3 + 6 = 18$ is divisible by 3.
 Eg: 72, 8448, 3972 etc.

6. Divisibility by 8

A number is divisible by 8 if last three digit of it is divisible by 8.
 Eg.: 47472 here 472 is divisible by 8 hence this number 47472 is divisible by 8.

7. Divisibility by 9

A number is divisible by 9 if the sum of its digit is divisible by 9.
 Eg.: 108936 here $1+0+8+9+3+6$ is 27 which is divisible by 9 and hence 108936 is divisible by 9.

8. Divisibility by 10

A number is divisible by 10 if its unit digit is 0.
 Eg.: 90, 900, 740, 34920 etc.

9. Divisibility by 11

A number is divisible by 11 if the difference of sum of digit at odd places and sum of digit at even places is either 0 or divisible by 11.
 Eg.: 1331, the sum of digits at odd place is $1+3$ and sum of digit at even places is $3+1$ and their difference is $4 - 4 = 0$. so 1331 is divisible by 11.

HCF and LCM of Numbers

H.C.F.

(Highest Common Factor) of two or more number is the greatest number that divides each one of them exactly. For example 8 is the highest common factor of 16 and 40.
 HCF is also called greatest common divisor (G.C.D.)

L.C.M.

(Least Common Multiple) of two or more number is the least or a lowest number which is exactly divisible by each of them.
 For example LCM of 8 and 12 is 24, because it is the first number which is multiple of both 8 and 12.

LCM and HCF of Fractions

Fractions are written in form of $\frac{\text{Numerator}}{\text{Denominator}}$. Where denominator is not equal to zero.

$$\text{H.C.F of Fraction} = \frac{(\text{H.C.F. of Numerators})}{(\text{LCM of Denominators})}$$

$$\text{L.C.M of Fraction} = \frac{(\text{LCM of Numerators})}{(\text{HCF of Denominators})}$$



Practice Exercise

- $$\sqrt{3\sqrt{80} + \frac{3}{9+4\sqrt{5}}} = ?$$

(a) $\sqrt{3\sqrt{5}}$ (b) 3
(c) $3\sqrt{3}$ (d) $3+2\sqrt{5}$
- x and y are integers and if $\frac{x^2}{y^3}$ is even integer then which of the following must be an even integer?
 (a) $x - y$ (b) $y + 1$
 (c) $\frac{x^2}{y^4}$ (d) xy
- What is the tens' digit of the sum of the first 50 terms of 1, 11, 111, 1111, 11111, 111111,?
 (a) 2 (b) 4
 (c) 5 (d) 8
- If $81^y = \frac{1}{27^x}$, in terms of y , $x = ?$
 (a) $\frac{3y}{4}$ (b) $-\frac{3y}{4}$
 (c) $\frac{4y}{3}$ (d) $-\frac{4y}{3}$
- If $\frac{1}{n+1} < \frac{1}{31} + \frac{1}{32} + \frac{1}{33} < \frac{1}{n}$; then $n = ?$
 (a) 9 (b) 10
 (c) 11 (d) 12
- If one integer is greater than another integer by 3, and the difference of their cubes is 117, what could be their sum?
 (a) 11 (b) 7
 (c) 8 (d) 9
- Which of these has total 24 positive factors?
 (a) $21^5 \times 2^3$ (b) $2^7 \times 12^3$
 (c) $2^6 \times 3^4$ (d) 63×55
- Two numbers, x and y are such that when divided by 6, they leave remainder 4 and 5 respectively. Find the remainder when $x^3 + y^3$ is divided by 6?
 (a) 2 (b) 3
 (c) 4 (d) 5
- What is the remainder when $N = (1! + 2! + 3! + \dots + 1000!)^{40}$ is divided by 10?
 (a) 1 (b) 3
 (c) 7 (d) 8
- Set A is formed by selecting some of the numbers from the first 100 natural numbers such that the HCF of any two numbers in the set A is 5, what is the maximum number elements that set A can have?
 (a) 7 (b) 8
 (c) 9 (d) 10
- Let x and y be positive integers such that x is prime and y is composite. Then,
 (a) $y - x$ cannot be an even integer
 (b) $\frac{x+y}{x}$ cannot be an even integer
 (c) $(x + y)$ cannot be even.
 (d) None of the above statements are true
- Let $N = 1421 \times 1423 \times 1425$. What is the remainder when N is divided by 12?
 (a) 0 (b) 9
 (c) 3 (d) 6
- When a four digit number is divided by 85 it leaves a remainder of 39. If the same number is divided by 17 the remainder would be ?
 (a) 2 (b) 5
 (c) 7 (d) 9
- Integers 34041 and 32506 when divided by a three-digit integer n leave the same remainder. What is n ?
 (a) 289 (b) 367
 (c) 453 (d) 307
- A box contains 100 tickets, numbered from 1 to 100. A person picks out three tickets from the box, such that the product of the numbers on two of the tickets yields the number on the third ticket. Which of the following tickets can never be picked as third ticket?
 (a) 10 (b) 12
 (c) 25 (d) 26
- N is a natural number, then how many values of N are possible such that $\frac{6N^3 + 3N^2 + N + 24}{N}$ is also a Natural Number?
 (a) 6 (b) 7
 (c) 8 (d) 9

17. What is the unit digit of $39^{53} \times 27^{23} \times 36^{12}$?
- (a) 2 (b) 4
(c) 6 (d) 8
18. How many number of zeros are there if we multiply all the prime numbers between 0 and 200.
- (a) 1 (b) 2
(c) 3 (d) 4
19. A man wrote all the natural numbers starting from 1 in a series. What will be the 50th digit of the number?
- (a) 1 (b) 2
(c) 3 (d) 4
20. $N = n(n+1)(n+2)(n+3)(n+4)$; where n is a natural number. Which of the following statement/s is/are true?
- Unit digit of N is 0.
 - N is perfectly divisible by 24.
 - N is perfect square.
 - N is odd.
- (a) 3 only (b) 3 and 4 only
(c) 1 only (d) 1 and 2 only
21. How many factors of $N = 12^{12} \times 14^{14} \times 15^{15}$ are multiple of $K = 12^{10} \times 14^{10} \times 15^{10}$
- (a) $2 \times 4 \times 5$ (b) $3 \times 5 \times 6$
(c) $8 \times 7 \times 4 \times 5$ (d) $9 \times 8 \times 6 \times 5$
22. In a certain base $137 + 254 = 402$ then What is the sum of $342 + 562$ in that base
- (a) 904 (b) 1014
(c) 1104 (d) 1024

Answers

1. (c) 2. (d) 3. (b) 4. (d) 5. (b)
6. (b) 7. (d) 8. (b) 9. (a) 10. (c)
11. (d) 12. (c) 13. (b) 14. (d) 15. (c)
16. (c) 17. (a) 18. (a) 19. (c) 20. (d)
21. (d) 22. (b)

Solutions

1. (c)

Method (i) $\sqrt{3\sqrt{80} + \frac{3}{9+4\sqrt{5}}}$ using rationalization

$$\begin{aligned}
 &= \sqrt{3\sqrt{80} + \frac{3}{9+4\sqrt{5}} \times \left(\frac{9-4\sqrt{5}}{9-4\sqrt{5}} \right)} \\
 &= \sqrt{3\sqrt{80} + \frac{(3 \times 9 - 3 \times 4\sqrt{5})}{9^2 - (4\sqrt{5})^2}} \\
 &= \sqrt{3\sqrt{80} + \frac{27 - 12\sqrt{5}}{81 - 80}} \\
 &= \sqrt{3\sqrt{16 \times 5} + 27 - 12\sqrt{5}} \\
 &= \sqrt{3 \times 4 \times \sqrt{5} + 27 - 12\sqrt{5}} \\
 &= \sqrt{12\sqrt{5} + 27 - 12\sqrt{5}} \\
 &= \sqrt{27} = 3\sqrt{3}
 \end{aligned}$$

Alternative Method

$$\begin{aligned}
 &\sqrt{\left(3\sqrt{80} + \frac{3}{9+4\sqrt{5}} \right)} \\
 3\sqrt{80} &\approx 3\sqrt{81} \approx 27 \\
 \text{and } \frac{3}{9+4\sqrt{5}} &< 1 \\
 \text{Thus, } \sqrt{3\sqrt{80} + \frac{3}{9+4\sqrt{5}}} &\approx \sqrt{3\sqrt{81}} \\
 &\approx \sqrt{3 \times 9} = 3\sqrt{3}
 \end{aligned}$$

2. (d)

if $\frac{x^2}{y^3} = \text{even}$
 $x^2 = y^3 \text{ even}$
 $\Rightarrow x^2 \Rightarrow \text{even}$
 and x is integer
 $\Rightarrow x = \text{even}$
 so only xy must be even.

3. (b)

$$\begin{array}{r}
 1 \\
 11 \\
 111 \\
 \vdots \\
 50 \text{ terms} \dots \dots \dots 111 \\
 \hline
 40
 \end{array}$$

unit digit $(1 + 1 \dots \dots 50 \text{ times}) = 0$

and carry = 5

tens digit $(1 + 1 + \dots \dots 49 \text{ times}) + \text{carry } 5 = 4$

4. (d)

$$\begin{aligned}
 81^y &= \frac{1}{27^x} \\
 \Rightarrow (3)^{4y} &= (3^{-3})^x \\
 \Rightarrow (3)^{4y} &= (3)^{-3x} \\
 \text{as } a^m &= a^n \\
 \text{and } a &\neq -1, 0, +1 \\
 \Rightarrow m &= n \\
 \text{so } 4y &= -3x \\
 x &= -\frac{4}{3}y
 \end{aligned}$$

5. (b)

$$\begin{aligned}
 \frac{1}{30} &> \frac{1}{33}; \frac{1}{30} > \frac{1}{31}; \frac{1}{30} > \frac{1}{31}; \\
 \Rightarrow \frac{1}{30} + \frac{1}{30} + \frac{1}{30} &> \frac{1}{31} + \frac{1}{32} + \frac{1}{33} \\
 \Rightarrow \frac{3}{30} &> \frac{1}{31} + \frac{1}{32} + \frac{1}{33} \\
 \Rightarrow \frac{1}{10} &> \frac{1}{31} + \frac{1}{32} + \frac{1}{33} \\
 \Rightarrow \frac{1}{n} &= \frac{1}{10} \Rightarrow n = 10
 \end{aligned}$$

and

$$\text{OR } \frac{1}{31} > \frac{1}{33}; \frac{1}{32} > \frac{1}{33}; \frac{1}{33} = \frac{1}{33}$$

$$\Rightarrow \frac{1}{31} + \frac{1}{32} + \frac{1}{33} > \frac{3}{33}$$

$$\Rightarrow \frac{1}{31} + \frac{1}{32} + \frac{1}{33} > \frac{1}{11} = \frac{1}{n+1}$$

$n = 10$

6. (b)

Use plugging in

$$\text{as } (x+3)^3 - x^3 = 117$$

$$x+3 \geq 5 \quad \text{as } (x+3)^3 \geq 117$$

$$\text{put } x = 2$$

$$\Rightarrow 5^3 - 2^3 = 125 - 8 = 117$$

$$\Rightarrow x = 2, \quad x+3 = 5$$

So, sum of both numbers = 7

Alternative Method

$$(x+3)^3 - x^3 = 117$$

$$x^3 + (3)^3 + 3(x)(3)(x+3) - x^3 = 117$$

$$x^3 + 27 + 27x + 9x^2 - x^3 = 117$$

$$\Rightarrow 9x^2 + 27x - 90 = 0$$

$$\Rightarrow x^2 + 3x - 10 = 0$$

$$\Rightarrow (x+5)(x-2) = 0$$

$$x = 2, -5$$

$$\Rightarrow \text{so either } 2, 5, \text{ or } -5, -2$$

$$\text{Thus sum} = 7, \text{ OR} = -7$$

7. (d)

Put in prime factorization theorem.

$$(a) \quad 21^5 \times 2^3 = 3^5 \times 7^5 \times 2^3$$

$$\text{Total factors} = 6 \times 6 \times 4 \neq 24$$

$$(b) \quad 2^7 \times (2^2 \times 3)^3 = 2^{13} \times 3^3$$

$$\text{Total factors} = 14 \times 4 \neq 24$$

$$(c) \quad 2^6 \times 3^4 = \text{factors } 7 \times 5 \neq 24$$

$$(d) \quad 63 \times 55 = 3^2 \times 7^1 \times 5^1 \times 11^1$$

$$\text{Factors} = 3 \times 2 \times 2 \times 2 = 24$$

8. (b)

$$\text{Rem} \frac{[x]}{6} = 4, \quad \text{Rem} \frac{[y]}{6} = 5$$

$$\begin{aligned}
 \text{Rem} &= \frac{[x^3 + y^3]}{6} = \frac{[4^3 + 5^3]}{6} \\
 &= \frac{[6 + 125]}{6}
 \end{aligned}$$

$$\Rightarrow \text{Rem} \left[\frac{4+5}{6} \right] = \text{Rem} \left(\frac{9}{6} \right) = 3$$

9. (a)

$$N = (1! + 2! + 3! + 4! + \dots + 1000!)$$

Now we have to check only

$1! + 2! + 3! + 4!$ as after that will factorial has unit digit as 0

$$5! = 120$$

$$6! = 720 \text{ and so on}$$

Thus unit digit of $(1! + 2! + 3! + 4! + 0)$ for all other

$$\Rightarrow (1 + 2 + 6 + 4 + 0)^{40}$$

Unit digits of all factorial

$$\Rightarrow (3)^{40} = (3)^{4k}$$

$\Rightarrow 3 \times 3 \times 3 \times 3 \Rightarrow 1$ unit digit. Hence when $(3)^{40} \div 10$, Remainder will be 1.

10. (c)

As there should be only 5 which should be common between any two number

so number may be $(5x_1, 5x_2, 5x_3, \dots, 5x_n)$

Previous GATE Solved Questions

(General Aptitude)

1. 25 persons are in a room. 15 of them play hockey, 17 of them play football and 10 of them play both hockey and football. Then the number of persons playing neither hockey nor football is
- (a) 2 (b) 17
(c) 13 (d) 3

[2010, 1 Mark]

2. If $137 + 276 = 435$ how much is $731 + 672$?
- (a) 534 (b) 1403
(c) 1623 (d) 1531

[2010, 2 Marks]

3. 5 skilled workers can build a wall in 20 days; 8 semiskilled workers can build a wall in 25 days; 10 unskilled workers can build a wall in 30 days. If a team has 2 skilled, 6 semiskilled and 5 unskilled workers, how long will it take to build the wall?
- (a) 20 days (b) 18 days
(c) 16 days (d) 15 days

[2010, 2 Marks]

4. Given digits 2, 2, 3, 3, 3, 4, 4, 4, 4 how many distinct 4 digit numbers greater than 3000 can be formed?
- (a) 50 (b) 51
(c) 52 (d) 54

[2010, 2 Marks]

5. Hari (H), Gita (G), Irfan (I) and Saira (S) are siblings (i.e. brothers and sisters). All were born on 1st January. The age difference between any two successive siblings (that is born one after another) is less than 3 years. Given the following facts:
1. Hari's age + Gita's age > Irfan's age + Saira's age.
 2. The age difference between Gita and Saira is 1 year. However, Gita is not the oldest and Saira is not the youngest.
 3. There are no twins.

In what order were they born (oldest first)?

- (a) HSI G (b) SGHI
(c) IGSH (d) IHSG

[2010, 2 Marks]

6. If $\text{Log}(P) = (1/2)\text{Log}(Q) = (1/3)\text{Log}(R)$, then which of the following options is TRUE?

- (a) $P^2 = Q^3R^2$ (b) $Q^2 = PR$
(c) $Q^2 = R^3P$ (d) $R = P^2Q^2$

[CE, ME, CS 2011, 1 Mark (Set-1)]

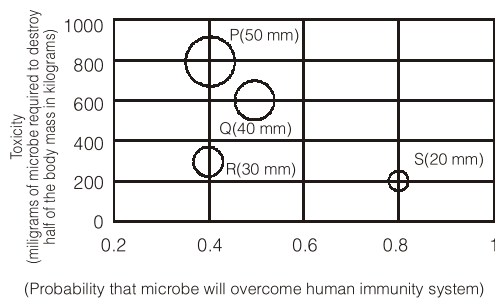
7. A container originally contains 10 litres of pure spirit. From this container 1 litre of spirit is replaced with 1 litre of water. Subsequently, 1 litre of the mixture is again replaced with 1 litre of water and this processes is repeated one more time. How much spirit is now left in the container?
- (a) 7.58 litres (b) 7.84 litres
(c) 7 litres (d) 7.29 litres

[CE, ME, CS 2011, 2 Marks (Set-1)]

8. The variable cost (V) of manufacturing a product varies according to the equation $V = 4q$, where q is the quantity produced. The fixed cost (F) of production of same product reduces with q according to the equation $F = 100/q$. How many units should be produced to minimize the total cost (V + F)?
- (a) 5 (b) 4
(c) 7 (d) 6

[CE, ME, CS 2011, 2 Marks (Set-1)]

9. P, Q, R and S are four types of dangerous microbes recently found in a human habitat. The area of each circle with its diameter printed in brackets represents the growth of a single microbe surviving human immunity system within 24 hours of entering the body. The danger to human beings varies proportionately with the toxicity, potency and growth attributed to a microbe shown in the figure below:



A pharmaceutical company is contemplating the development of a vaccine against the most dangerous microbe. Which microbe should the company target in its first attempt?

- (a) P (b) Q
(c) R (d) S

[CE, ME, CS 2011, 2 Marks (Set-1)]

10. A transporter receives the same number of orders each day. Currently, he has some pending orders (backlog) to be shipped. If he uses 7 trucks, then at the end of the 4th day he can clear all the orders. Alternatively, if he uses only 3 trucks, then all the orders are cleared at the end of the 10th day. What is the minimum number of trucks required so that there will be no pending order at the end of the 5th day?

- (a) 4 (b) 5
(c) 6 (d) 7

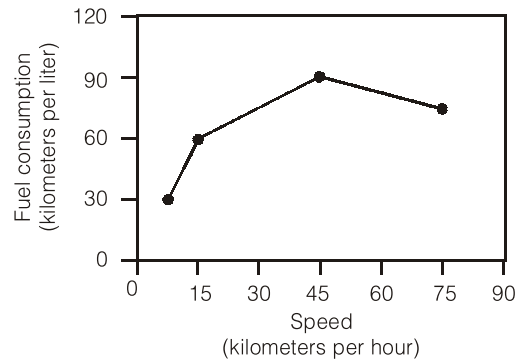
[CE, ME, CS 2011, 2 Marks (Set-1)]

11. There are two candidates P and Q in an election. During the campaign 40% of the voters promised to vote for P, and rest for Q. However, on the day of election 15% of the voters went back on their promise to vote for P and instead voted for Q. 25% of the voters went back on their promise to vote for Q and instead voted for P. Suppose, P lost by 2 votes, then what was the total number of voters?

- (a) 100 (b) 110
(c) 90 (d) 95

[EE, EC 2011, 1 Mark (Set-2)]

12. The fuel consumed by a motorcycle during a journey while travelling at various speeds is indicated in the graph below



The distance covered during four laps of the journey are listed in the table below:

Lap	Distance (kilometers)	Average speed (kilometers per hour)
P	15	15
Q	75	45
R	40	75
S	10	10

From the given data, we can conclude that the fuel consumed per kilometre was least during the lap

- (a) P (b) Q
(c) R (d) S

[EE, EC 2011, 2 Marks (Set-2)]

13. Three friends, R, S and T shared toffee from a bowl. R took $\frac{1}{3}$ rd of the toffees, but returned four to the bowl. S took $\frac{1}{4}$ th of what was left but returned three toffees to the bowl. T took half of the remainder but returned two back into the bowl. If the bowl had 17 toffees left, how many toffees were originally there in the bowl?

- (a) 38 (b) 31
(c) 48 (d) 41

[EE, EC 2011, 2 Marks (Set-2)]

14. Given that $f(y) = |y|/y$, and q is any non-zero real number, the value of $|f(q) - f(-q)|$ is

- (a) 0 (b) -1
(c) 1 (d) 2

[EE, EC 2011, 2 Marks (Set-2)]

15. The sum of n terms of the series $4 + 44 + 444 + \dots$ is

- (a) $(4/81) [10^{n+1} - 9n - 1]$
(b) $(4/81) [10^{n-1} - 9n - 1]$

ANSWER KEY

1. (d)	38. (d)	75. (d)	112. (b)	149. (b)	186. (a)
2. (c)	39. (b)	76. (140)	113. (a)	150. (c)	187. (c)
3. (d)	40. (a)	77. (a)	114. (a)	151. (a)	188. (b)
4. (b)	41. (a)	78. (c)	115. (32)	152. (d)	189. (b)
5. (b)	42. (16)	79. (c)	116. (c)	153. (c)	190. (b)
6. (b)	43. (d)	80. (d)	117. (c)	154. (b)	191. (b)
7. (d)	44. (b)	81. (c)	118. (a)	155. (a)	192. (d)
8. (a)	45. (560)	82. (c)	119. (c)	156. (d)	193. (d)
9. (d)	46. (d)	83. (c)	120. (c)	157. (b)	194. (c)
10. (c)	47. (b)	84. (1300)	121. (3)	158. (d)	195. (c)
11. (a)	48. (b)	85. (d)	122. (d)	159. (b)	196. (d)
12. (b)	49. (45)	86. (b)	123. (b)	160. (b)	197. (b)
13. (c)	50. (c)	87. (180)	124. (d)	161. (a)	198. (b)
14. (d)	51. (163)	88. (d)	125. (b)	162. (d)	199. (a)
15. (c)	52. (d)	89. (b)	126. (800)	163. (a)	200. (c)
16. (a)	53. (a)	90. (25)	127. (a)	164. (c)	201. (a)
17. (b)	54. (16)	91. (a)	128. (c)	165. (c)	202. (a)
18. (b)	55. (d)	92. (a)	129. (b)	166. (a)	203. (b)
19. (c)	56. (b)	93. (d)	130. (c)	167. (a)	204. (a)
20. (a)	57. (d)	94. (c)	131. (2.064)	168. (d)	205. (d)
21. (d)	58. (4)	95. (0.4896)	132. (b)	169. (b)	206. (b)
22. (a)	59. (20000)	96. (b)	133. (b)	170. (d)	207. (c)
23. (c)	60. (0.81)	97. (c)	134. (280)	171. (c)	208. (b)
24. (d)	61. (a)	98. (4.54)	135. (c)	172. (b)	209. (c)
25. (a)	62. (495)	99. (b)	136. (b)	173. (c)	210. (c)
26. (d)	63. (c)	100. (b)	137. (c)	174. (a)	211. (d)
27. (a)	64. (b)	101. (b)	138. (a)	175. (7)	212. (c)
28. (d)	65. (b)	102. (a)	139. (c)	176. (120)	213. (c)
29. (b)	66. (22)	103. (d)	140. (c)	177. (c)	214. (b)
30. (a)	67. (b)	104. (4536)	141. (d)	178. (b)	215. (d)
31. (c)	68. (96)	105. (d)	142. (c)	179. (c)	216. (a)
32. (d)	69. (d)	106. (a)	143. (c)	180. (c)	217. (d)
33. (c)	70. (850)	107. (c)	144. (c)	181. (a)	218. (a)
34. (b)	71. (48)	108. (c)	145. (b)	182. (c)	219. (b)
35. (b)	72. (6)	109. (b)	146. (d)	183. (d)	220. (c)
36. (c)	73. (b)	110. (8)	147. (d)	184. (d)	221. (c)
37. (c)	74. (c)	111. (a)	148. (c)	185. (c)	222. (a)

EXPLANATIONS

1. (d)

Using the set theory formula

 $n(A)$: Number of people who play hockey = 15 $n(B)$: Number of people who play football = 17 $n(A \cap B)$: Persons who play both hockey and football = 10 $n(A \cup B)$: Persons who play either hockey or football or both

Using the formula

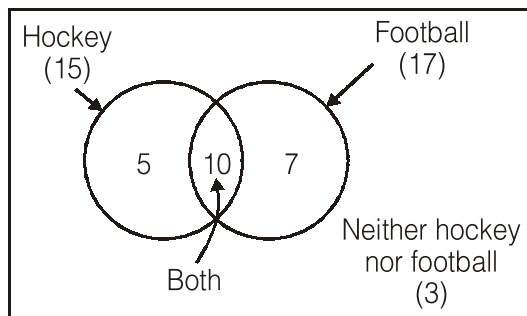
$$n(A \cup B) = n(A) + n(B) - n(A \cap B)$$

$$n(A \cup B) = 15 + 17 - 10 = 22$$

Thus people who play neither hockey nor football
 $= 25 - 22 = 3$

Alternative Method

Refer to Venn diagram given below:



Number of people playing nither of the two games is equal to 3.

2. (c)

$$137 + 276 = 435$$

This an addition on base 8.

$$\text{Hence, } 731 + 672(8) = 1623$$

Alternative Method

7 and 6 added is becoming five means the given two numbers are added on base 8.

$$\begin{array}{r} (137)_8 \\ + (276)_8 \\ \hline (435)_8 \end{array}$$

Hence we have to add the another two given set of numbers also on base 8.

$$\begin{array}{r} (731)_8 \\ + (672)_8 \\ \hline (1623)_8 \end{array}$$

Hence the overall problem was based on identifyng base, which was 8, and adding number on base 8.

3. (d)

$$\text{Per day work or rate of 5 skilled workers} = \frac{1}{20}$$

$$\Rightarrow \text{Per day work or rate of one skill worker}$$

$$= \frac{1}{5 \times 20} = \frac{1}{100}$$

$$\text{Similarly Per day work or rate of 8 semiskilled workers} = \frac{1}{25}$$

$$\Rightarrow \text{Per day work or rate of one semi-skill worker}$$

$$= \frac{1}{8 \times 25} = \frac{1}{200}$$

$$\text{And per day work or rate of 10 unskilled workers}$$

$$= \frac{1}{30}$$

$$\Rightarrow \text{Per day work or rate of one semi-skill worker}$$

$$= \frac{1}{10 \times 30} = \frac{1}{300}$$

Thus total per day work of 2 skilled, 6 semiskilled and 5 unskilled workers

$$= \frac{2}{100} + \frac{6}{200} + \frac{5}{300} = \frac{12 + 18 + 10}{600}$$

$$= \frac{40}{600} = \frac{1}{15}$$

Thus time to complete the work is 15 days.

Alternative Method

Let one day work of skilled semi-skilled and unskilled worker be a, b, c units respectively.

$$5a \times 20 = 8b + 25 = 10c \times 30 = \text{Total unit of work}$$

$$100a = 200b = 300c$$

$$a = 2b = 3c$$

$$\Rightarrow b = \frac{a}{2} \text{ and } c = \frac{a}{3}$$

Given that 2 skilled, 6 semi-skilled and 5 unskilled workers are working. Let they finish the work in 'x' days.

$$(2a + 6b + 5c)x = 5a \times 20$$

= Total units of work

$$\left(2a + 3a + \frac{5}{3}a\right)x = 5a \times 20$$

$$\frac{20a}{3}x = 5a \times 20$$

$$x = 15 \text{ days}$$

4. (b)

We have to make 4 digit numbers, so the number should be start with 3 or 4, two cases possible;

Case (1) thousands digit is 3

Now other three digits may be any of 2, 2, 3, 3, 4, 4, 4, 4.

(a) Using 2, 2, 3
 $\Rightarrow 223, 232, 322$ -----

$$\left(\frac{3!}{2!} = 3 \text{ numbers are possible}\right)$$

(b) Using 2, 2, 4 $\Rightarrow 224, 242, 422$

$$\left(\frac{3!}{2!} = 3 \text{ numbers are possible}\right)$$

(c) Using 2, 3, 3 $\Rightarrow 233, 323, 332$

$$\left(\frac{3!}{2!} = 3 \text{ numbers are possible}\right)$$

(d) Using 2, 3, 4 $\Rightarrow 234, 243, 324, 342, 423, 432$

$$(3! = 6 \text{ numbers are possible})$$

(e) Using 2, 4, 4 $\Rightarrow 244, 424, 442$

$$\left(\frac{3!}{2!} = 3 \text{ numbers are possible}\right)$$

(f) Using 3, 3, 4 $\Rightarrow 334, 343, 433$

$$\left(\frac{3!}{2!} = 3 \text{ numbers are possible}\right)$$

(g) Using 3, 4, 4 $\Rightarrow 344, 434, 443$

$$\left(\frac{3!}{2!} = 3 \text{ numbers are possible}\right)$$

(h) Using 4, 4, 4 $\Rightarrow 444$

$$\left(\frac{3!}{3!} = 1 \text{ number is possible}\right)$$

Total 4 digit numbers in case 1 = $3 + 3 + 3 + 6 + 3 + 3 + 3 + 1 = 25$

Case (2) thousands digit is 4 ; Now other three digits may be any of 2, 2, 3, 3, 3, 4, 4, 4.

(a) Using 2, 2, 3 $\Rightarrow 223, 232, 322$

$$\left(\frac{3!}{2!} = 3 \text{ numbers are possible}\right)$$

(b) Using 2, 2, 4 $\Rightarrow 224, 242, 422$

$$\left(\frac{3!}{2!} = 3 \text{ numbers are possible}\right)$$

(c) Using 2, 3, 3 $\Rightarrow 233, 323, 332$

$$\left(\frac{3!}{2!} = 3 \text{ numbers are possible}\right)$$

(d) Using 2, 3, 4 $\Rightarrow 234, 243, 324, 342, 423, 432$

$$\left(\frac{3!}{2!} = 3 \text{ numbers are possible}\right)$$

(e) Using 2, 4, 4 $\Rightarrow 244, 424, 442$

$$\left(\frac{3!}{2!} = 3 \text{ numbers are possible}\right)$$

(f) Using 3, 3, 3 $\Rightarrow 333$

$$\left(\frac{3!}{3!} = 1 \text{ number is possible}\right)$$

(g) Using 3, 3, 4 $\Rightarrow 334, 343, 433$

$$\left(\frac{3!}{2!} = 3 \text{ numbers are possible}\right)$$

(h) Using 3, 4, 4 $\Rightarrow 344, 434, 443$

$$\left(\frac{3!}{2!} = 3 \text{ numbers are possible}\right)$$

(i) Using 4, 4, 4 $\Rightarrow 444$

$$\left(\frac{3!}{3!} = 1 \text{ number is possible}\right)$$

Total 4 digit numbers in case 2 = $3 + 3 + 3 + 6 + 3 + 3$
 $= 1 + 3 + 1 = 26$

Thus total 4 digits numbers using case (1) and case (2)
 $= 25 + 26 = 51$

*** Alternative Method / Shortcut method**

As the number is greater than 3000. So thousand's place can be tiehr 3 or 4. Let's consider the following two cases

Case (I) When thousand's place is 3.

3 a b c

If there is no restriction on number of two's, three's and four's. Then each of a, b, c can be filled with 2 or 3 or 4 each in 3 ways.

So $3 \times 3 \times 3 = 27$ numbers are there. Out of which 3222, 3333 are invalid as 2 can be used twice & three thrice only so number of such valid numbers beginning with 3 are $27 - 2 = 25$ (i)

Case (II) When thousand's place is 4

4 a b c

Without restriction on number of 2's, 3's and 4's a, b, c (as explained in case I) can be filled in 27 ways.

Out of these 27 numbers, 4222 is only invalid as two have to be used twice only.

So valid numbers are $27 - 1 = 26$ (ii)

Total numbers from Case (I) & Case (II) $25 + 26 = 51$.

5. (b)

Suppose: Hari's age : H, Gita's age : G,

Saira's age : S, Irfan's age : I

- $H + G > I + S$
- Using Statement (2) both $G - S = 1$ or $S - G = 1$; G can't be oldest and S can't be youngest.
- There are no twins thus using statement (2) either GS or SG possible.

(A) HSI: not possible as there is I between S and G which is not possible using statement (3)

(B) SGHI: SG order is possible, $S > G > H > I$ and $G + H > S + I$ (possible) Because if $\{ S = G + 1; \text{ and } G = H + 1 \text{ and } H = I + 2 \}$ then $G + (I + 2) > (G + 1) + I$

(C) IGSH: according to this $I > G$ and $S > H$ thus adding these both inequalities we get $I + S > G + H$ which is opposite of statement (2) thus not possible.

(D) IHSG: according to this $I > H$ and $S > G$ thus adding both inequalities $I + S > H + G$ which is opposite of statement (2). Thus not possible.

6. (b)

$$\log(P) = \frac{1}{2} \log(Q) = \frac{1}{3} \log(R)$$

$$\Rightarrow \log(P) = \log(Q)^{1/2} \\ = \log(R)^{1/3} = K$$

$$\Rightarrow P = (Q)^{1/2} = (R)^{1/3} = K$$

$$\Rightarrow P = K, Q = K^2, R = K^3 \quad \dots (i)$$

Now, only option (B) $Q^2 = PR$ satisfies

$$Q^2 = (K^2)^2 = K^4 \quad \text{From } \dots (i)$$

$$P.R = K * K^3 = K^4 \quad \text{From } \dots (i)$$

Here, $Q^2 = PR$ holds true

7. (d)

Shortcut Method

Every time if we take 1 litre of mixture out and replace with water, content of pure spirit will keep on reducing by 10%.

So, final quantity of spirit after 3 such operations are

$$10 \times 0.9 \times 0.9 \times 0.9 = 7.29 \text{ litres}$$

Alternative Solution

$$\frac{\text{Quantity of spirit left after } n^{\text{th}} \text{ operation}}{\text{Initial quantity of spirit}}$$

$$= \left(\frac{a-b}{a} \right)^n = \left(1 - \frac{b}{a} \right)^n$$

where 'a' is initial quantity of pure spirit and 'b' is quantity taken out and replaced every time.

Hence, quantity of spirit left after 3rd operation

$$= \text{initial quantity} \times \left(1 - \frac{1}{10} \right)^3$$

$$= 10 \times 0.9 \times 0.9 \times 0.9$$

$$= 7.29 \text{ litres}$$

8. (a)

(T.C.) Total cost = $V + f$

$$T.C = 4q + \frac{100}{q}$$

As we have to minimize total cost.

Using options

$$(a) \quad q = 5, T.C. = 4 \times 5 + \frac{100}{5} = 40$$

$$(b) \quad q = 4, T.C. = 4 \times 4 + \frac{100}{4} = 41$$

$$(c) \quad q = 7, T.C. = 4 \times 7 + \frac{100}{7} = 42.285$$

$$(d) \quad q = 6, T.C. = 4 \times 6 + \frac{100}{6} = 40.\overline{66}$$

Hence, T.C. is minimum at $q = 5$, **(a) ans.**

* always put options to get answer fast.

Previous ESE Prelims Solved Questions

(General Aptitude)

1. Three hundred passengers are travelling in white, silver and black cars; each of these cars is carrying 6, 5 and 3 passengers, respectively. If the number of white and silver cars is equal and there is only one black car, what is the total number of cars?

(a) 52 (b) 53
(c) 54 (d) 55

[ESE Pre-2017]

2. The present ages of 3 brothers are in the proportion 3 : 4 : 5. After 10 years the sum of their ages will be 78. What are their ages now?

(a) 12, 16 and 20 (b) 15, 20 and 25
(c) 21, 28 and 35 (d) 24, 32 and 40

[ESE Pre-2017]

3. A total of 324 notes comprising of ₹ 20 and ₹ 50 denominations make a sum of ₹ 12,450. The number of ₹ 20 notes is

(a) 200 (b) 144
(c) 125 (d) 110

[ESE Pre-2017]

4. Five Men can paint a building in 20 days, 8 Women can paint the same building in 25 days and 10 Boys can paint it in 30 days. If a team has 2 Men, 6 Women and 5 Boys, how long will it take to paint the building?

(a) 12 days (b) 13 days
(c) 14 days (d) 15 days

[ESE Pre-2017]

5. Rajiv spends 40% of his salary on food, 20% on house rent, 10% on entertainment and 10% on conveyance. If his savings at the month end are ₹ 2,000, then his monthly salary is:

(a) ₹ 6,000 (b) ₹ 8,000
(c) ₹ 10,000 (d) ₹ 12,000

[ESE Pre-2017]

6. A group of workers estimate to finish a work in 10 days, but 5 workers could not join the work.

If the rest of them finished the work in 12 days, the number of members present in the team originally is

(a) 50 (b) 45
(c) 35 (d) 30

[ESE Pre-2017]

7. The sum of squares of successive integers 8 to 16, both inclusive, will be

(a) 1126 (b) 1174
(c) 1292 (d) 1356

[ESE Pre-2018]

8. Given that 0.8 is one root of the equation, $x^3 - 0.6x^2 - 1.84x + 1.344 = 0$. The other roots of this equation will be

(a) 1.1 and -1.4 (b) -1.2 and 1.4
(c) 1.2 and -1.4 (d) -1.1 and 1.4

[ESE Pre-2018]

9. The equation, $x^3 - 8x^2 + 37x - 50 = 0$ is factored and it has $(3 + 4i)$ as one of its roots. What is the real root of this equation?

(a) 2 (b) 4
(c) 6.5 (d) 13

[ESE Pre-2018]

10. Circle A is 4 cm in diameter; circle B is 5 cm in diameter. Circle C has its circumference equal to the sum of the circumferences of both A and B together. What will be the ratio of the area of circle C, with respect to the area of circle A and circle B respectively?

(a) 5.0625 and 1.84 (b) 3.875 and 1.84
(c) 5.0625 and 3.24 (d) 3.875 and 3.24

[ESE Pre-2018]

11. The 12 digits on the face of a clock are to be represented employing contributions of only the number 9 as either 9 or $\sqrt{9}$. The other prescribed conditions are (i) the least number of uses alone are permitted; and (ii) when alternates are possible,

use of 9 will be preferred over use of $\sqrt{9}$, which should be used minimally. How many times would $\sqrt{9}$ have to be used?

- (a) 6 (b) 5
(c) 4 (d) 3

[ESE Pre-2018]

12. In a particular test, the marks scored by 4 candidates – A, B, C and D are as follows:

- Marks obtained by A and B add to 100;
- Marks obtained by C and D add up to those scored by A;
- B scores 4 times of D;
- D scores 10 marks less than C.

The marks obtained by C will be

- (a) 30 (b) 15
(c) 20 (d) 25

[ESE Pre-2018]

13. What is the form of the function $f(x)$ for the following data?

x	0	1	2	3
$f(x)$	3	6	11	18

- (a) $x^2 + 2x + 3$ (b) $x^2 - 2x + 3$
(c) $x^2 + 2x - 3$ (d) $x^2 - 2x - 3$

14. What is the maximum value of z , if $z = 10x + 6y$ subject to the constraints $3x + y \leq 12$, $2x + 5y \leq 34$, $x \geq 0$, $y \geq 0$?

- (a) 56 (b) 52
(c) 50 (d) 40

[ESE Pre-2018]

15. Let the sum of the squares of successive integers 0, 1, 2, ..., $n - 1$, n be denoted by S . Let the sum of the cubes of the same integers be denoted by C . It is desirable that $\frac{C}{S}$, as n increases in steps of 'unity' from 'zero', is given by the series:

$\frac{0}{1}, \frac{3}{3}, \frac{9}{5}, \frac{18}{7}, \frac{30}{9}, \dots$ (for $n = 0, 1, 2, 3, 4, \dots$). What

will this ratio be for $n = 8$?

- (a) $\frac{108}{17}$ (b) $\frac{103}{17}$
(c) $\frac{103}{15}$ (d) $\frac{100}{15}$

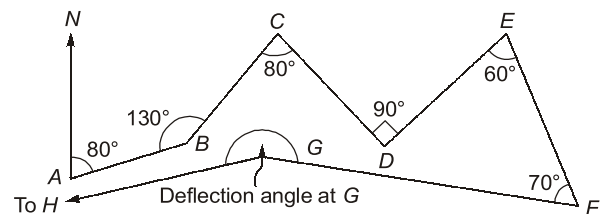
[ESE Pre-2018]

16. A wall, rectangular in shape, has a perimeter of 72 m. If the length of its diagonal is 18 m, what is the area of the wall?

- (a) 224 m^2 (b) 486 m^2
(c) 572 m^2 (d) 606 m^2

[ESE Pre-2018]

17. To isolate an enclosed area for conservation, an open traverse is run keeping close to (but outside of) the exterior boundary of the area through ground points $A \rightarrow B \rightarrow C \rightarrow D \rightarrow E \rightarrow F \rightarrow G \rightarrow$ towards H (to be eventually located). AB is 80° to the East of the North line at A . Deflection/Interior angles at B, C, D, E, F are indicated. What would be the magnitude of the deflection angle at G (as marked) so that GH may run parallel to BA ? (Lengths are immaterial in this case.)



- (a) 190° (b) 210°
(c) 200° (d) 230°

[ESE Pre-2018]

18. The objective function $z = 3x_1 + 5x_2$ is to be maximized subjected to constraints.

$$x_1 + 2x_2 \leq 200$$

$$x_1 + x_2 \leq 150$$

$$x_1, x_2 \geq 0$$

The values of x_1 and x_2 in this context are, respectively

- (a) 100 and 75 (b) 125 and 75
(c) 100 and 50 (d) 125 and 50

[ESE Pre-2018]

19. Consider the length of a room is 15 m and width is 10 m. If the sum of the areas of the floor and ceiling is equal to the sum of the areas of the four walls, then the volume of the room is

- (a) 900 m^3 (b) 1000 m^3
(c) 1200 m^3 (d) 1500 m^3

[ESE Pre-2018]

ANSWER KEY

- | | | | | | | | | |
|---------|---------|---------|---------|---------|---------|---------|---------|---------|
| 1. (d) | 2. (a) | 3. (c) | 4. (d) | 5. (c) | 6. (d) | 7. (d) | 8. (c) | 9. (a) |
| 10. (c) | 11. (b) | 12. (d) | 13. (a) | 14. (a) | 15. (a) | 16. (b) | 17. (a) | 18. (c) |
| 19. (a) | 20. (a) | 21. (b) | 22. (b) | 23. (a) | 24. (b) | 25. (c) | 26. (a) | 27. (c) |
| 28. (b) | 29. (c) | 30. (d) | 31. (a) | 32. (c) | 33. (d) | 34. (b) | 35. (b) | 36. (c) |
| 37. (b) | 38. (c) | 39. (a) | 40. (c) | 41. (b) | 42. (c) | 43. (c) | 44. (a) | 45. (a) |
| 46. (c) | 47. (c) | 48. (b) | 49. (b) | 50. (d) | 51. (c) | 52. (b) | 53. (c) | 54. (b) |
| 55. (d) | 56. (a) | 57. (d) | 58. (a) | 59. (b) | 60. (c) | 61. (d) | 62. (a) | 63. (b) |
| 64. (a) | 65. (d) | 66. (b) | 67. (b) | 68. (d) | 69. (d) | 70. (b) | 71. (c) | 72. (d) |
| 73. (c) | 74. (b) | 75. (b) | 76. (c) | 77. (b) | 78. (b) | 79. (*) | 80. (d) | 81. (b) |
| 82. (d) | | | | | | | | |

EXPLANATIONS

1. (d)

Since the number of passengers in Black car is 3, it leaves $300 - 3 = 297$ passengers to be accommodated in White and Silver coloured cars which are equal in number ($W = S$).

We can form a linear equation:

$$(6 + 5)W = 297 \text{ giving } W = 27 \text{ as also } S = 27$$

$$\text{Total number of cars being } 27 + 27 + 1 = 55$$

2. (a)

Let $3x$, $4x$, $5x$ be the present age of 3 brothers. After 10 years, sum of their age is $12x + 30 = 78$ which gives $x = 4$

Hence the present age of three brothers is 12, 16 and 20 years.

Alt: Can be directly solved using the given options since the sum of their present age = $78 - 30 = 48$ which is satisfied by option 'A' alone.

3. (c)

We can form 2 linear equations taking the number of Rs. 20 and Rs. 50 notes as T and F

$$T + F = 324 \quad \dots(1)$$

$$20T + 50F = 12450 \quad \dots(2)$$

Solving the 2 equations, we get $T = 125$

Alt 1: If all the notes are Rs. 50 notes, total amount = $324 \times 50 = \text{Rs. } 16200$ which is $16200 - 12450 = 3750$

$$3750/(50 - 20) = 125 \text{ notes of Rs. } 20.$$

Alt 2: This question can also be solved by putting options.

4. (d)

5 men in 20 days = 100 man days

8 women in 25 days = 200 woman days

10 boys in 30 days = 300 boy days

which means $100 \text{ MD} = 200 \text{ WD} = 300 \text{ BD}$ or
1 man day = 3 boy days; 1 woman day = 1.5 Boy days

2 men, 6 women and 5 boys = $2 \times 3 + 6 \times 1.5 + 5 = 20$ boys deployed to complete the task which will get completed in $300/20 = 15$ days

$$\text{Alt: } [2(1/100) + 6(1/200) + 5(1/300)]x = 1$$

Which gives $x = 15$

5. (c)

The remaining percentage after expenditure 20% which equals Rs. 2000 leading to total monthly income = Rs. 10000.